

iv. Sample paper

Estimating U.S. Class-A pan evaporation from few climate data

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Abstract

In view of the shortage of good measurements of lake evaporation for testing a new estimation formula, a modification of the formula has been devised which can be compared with US Class-A pan measurements, which are available widely. Both formulae, for lake and pan evaporation respectively, are based on Penman's evaporation equation and are for use when the only reliable data that are available are daily extreme temperatures, for instance. The pan-evaporation formula allows for the geometry of a US Class-A pan evaporimeter, and for the wetness and albedo of its surroundings, without requiring any empirical calibration based on evaporation measurements. The resulting equation for the monthly mean pan-evaporation rate (the so-called \diamond Penpan \diamond formula) includes an estimate of the solar irradiance, which may be obtained from the extra-terrestrial radiation and the cloudiness, derived from rainfall figures. The estimates of evaporation differ from measurements with pans at nine places around the world by about 0.6 mm.d-1.

Introduction

Many weather stations include measurements of the evaporation from a US Class-A pan [1], as the basis for calculating the water loss from lakes or from crops [2, 3]. But most places are without such measurements, and, even where there is a pan, the measurements may be vitiated by poor maintenance, leading to errors due to leaks, the growth of algae in the water, an incorrect water level, weed-growth nearby, and so on. Also, it is hard to measure evaporation accurately during rainfall [4], perhaps because of splashing of water in or out of the pan. In view of these difficulties, it would be useful and cheaper to have some means of estimating pan evaporation with reasonable accuracy, from reliable climate measurements, such as temperatures [5]. Such estimates could provide values for places between those with reliable measurements, and facilitate a check on doubtful measurements.

Previous work

The chief use of pan-evaporation data E_p lies in estimating lake evaporation E_o (or else the potential crop evaporation rate E_t) by means of empirical factors. Parallel simultaneous measurements of E_p and E_o , for instance, yield the \diamond pan coefficient \diamond E_o/E_p [6 - 8], and a knowledge of this factor, plus local pan measurements, give an estimate for E_o . Regrettably, the pan coefficient for a US Class A pan, for instance, has values widely scattered around 0.77, as shown by the eighteen papers listed in **Appendix 1**. It varies seasonally because of the lag of lake temperature [7] and increases linearly with the relative humidity, from 0.62 - 0.80 [9]. Such variability has caused this method of deriving E_o (or E_t) to be replaced by direct estimation, preferably by means of the well-known equation of Penman [10].

Measurements of pan evaporation E_p are compared with Penman estimates of lake evaporation E_{Pen} in **Fig 1**, from data in a review by Stanhill [11]. This shows twelve monthly-mean values from each of a dozen places around the world, indicating that E_{Pen} is less than E_p , especially at high evaporation rates. A rough figure for E_{Pen}/E_p is seen to be about 0.7, but the curvature of a line through the points demonstrates again that the ratio is not a constant. Also, the scatter of the points implies that no lake-evaporation formula based on Penman's original equation can be tested usefully by means of pan measurements.

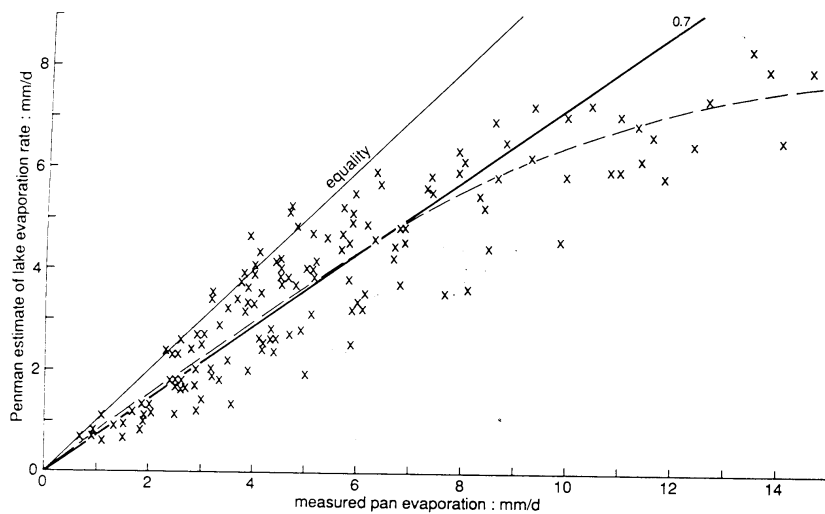


Fig 1. Comparison of Penman estimates of monthly mean lake evaporation rates at twelve places, with US Class-A pan evaporimeter measurements there, using data given by Stanhill [11].

A disadvantage of the the Penman formula for E_o is that it requires measurements of temperature, humidity, wind and net irradiance, which are not all everywhere available. This was discussed in a previous paper [12], leading to the following simplified version -

$$E_o = (0.015 + 0.00042 T + 10^{-6}z) (0.8 R_s - 40) + 2.5 F u [T - T_d]) \quad \text{mm.d}^{-1} \quad (1)$$

where T is the average of the daily extreme Celsius temperatures, z the elevation (m), F allows for the change of air density with elevation and stands for $[1.0 - 8.7 \times 10^{-5} z]$, u is the wind speed (m.s^{-1}) at 2 m, T_d is the dewpoint temperature and R_s the solar irradiance of the lake's surface (W.m^{-2}). The dewpoint can be estimated graphically from the daily extreme temperatures [13]. As regards R_s , two methods of estimating it were described earlier [12]. The more accurate method requires monthly rainfall data, as proxy for the cloud which cuts out some of the extra-terrestrial radiation, given in a table [14]. Often it is sufficient to estimate the wind speed approximately from measurements nearby or at other times, since evaporation varies much less than proportionally with changes of wind [3, 13]. Eqn 1 shows that the dependence on wind is least when radiation is strong. Consequently, only daily extreme temperature measurements are essential, with rainfall and wind speed data as desirable. Errors of estimating E_o with Eqn 1 were shown to be around 0.3 mm.d^{-1} at Copenhagen, for example.

Unfortunately, there are only a few reliable sets of lake-evaporation measurements for checking Eqn 1, whereas there are many measurements of pan evaporation E_p , from all over the world. So it is useful to modify the lake-evaporation equation to the case of a pan, to facilitate testing the universality of Eqn 1. That is the main purpose of the present paper.

Theory

Altering Eqn 1 to give the pan-evaporation rate E_p involves the geometry of the raised, circular pan, which affects its solar irradiance and advective heat transfer. The US Class-A pan is 1.21 m in diameter (so that the water surface has an area of 1.15 m^2) with a wall 255 mm high (ie its outside area is 0.97 m^2), and therefore the vertical section through a diameter has an area of 0.31 m^2 .

Sometimes the pan is screened by wire mesh to prevent birds and animals from drinking the water, especially in arid climates. This reduces the wind and radiation over the water's surface and consequently lowers the evaporation rate, depending on the size of the mesh. The reduction may be about 13% in a humid climate [15], or 10% in a semi-arid climate [16, 17].

The rate of pan evaporation depends on the input of energy, chiefly solar radiation. In addition to the solar radiation at the water surface of a pan, there is also a considerable transfer of heat through the wall, which affects the water's temperature and hence its rate of evaporation. Insulating the wall and base reduces evaporation by as much as 29% [18]. Heat through the wall consists partly of radiation, and partly advection from the wind around. As regards the extra irradiance, there are four factors - a) exposure of the wall to direct sunshine, b) diffuse radiation from the sky onto the wall, c) solar radiation reflected onto the wall from the ground around, and d) longwave radiation from the surroundings. All this additional heating more than offsets the reduction of evaporation due to the albedo of a pan being about 14%, instead of 7% for water [13]. We will now consider the four factors.

a) The direct radiation in the total solar irradiance of the ground depends on the amount of cloud and on the Sun's elevation in the sky. When the Sun is at an angle Q above the horizon, it sees an area of a US Class-A pan equal to $[0.31 \cos Q + 1.15 \sin Q]$ m², including what is seen of the wall. Integration of the expression over a whole day, for the case of the Sun at the equator at the time of the equinox (when the Sun rises to 90 degrees at noon), shows that the subtended area is 1.27 times the area of the water alone, on average. This ratio may be called the pan radiation factor P. (The integration of the bracketed sum can be done by calculating Q for each hour of the day at any particular latitude Δ [13] and then adding the daily total. This is compared with the similar integral of $[1.15 \sin Q]$, to obtain P.) For these calculations it is assumed as an approximation that each daytime lasts twelve hours, the annual average.

The annual swing of the Sun's path between the Tropics means that P at latitude 38 $^{\circ}$, for instance, ranges from 1.35, the value at 15 $^{\circ}$ (ie 38 - 23) in summer, to 1.66 at 61 $^{\circ}$ (ie 38 + 23) in winter. However, once again we will take the average throughout the year, the value for 38 $^{\circ}$ in this case, which is 1.46.

The annual average departure from overhead of the Sun's midday angle varies from 11.7 degrees at the equator (ie half the angle of the Tropics), to 13.9 at 10 $^{\circ}$ latitude, 16.5 at 15 $^{\circ}$, and 20.3 at 20 $^{\circ}$. In other words, the average departure at 10 $^{\circ}$, say, is what it would be at 13.9 $^{\circ}$ if there were no annual swing of the Sun's path. In general, it can be shown graphically that the average departure from the equator at latitudes between the Tropics is about $[(23.5 + \Delta)^2 + (23.5 - \Delta)^2]/[4 \times 23.5]$. This correction at low latitudes has been incorporated into the following equation, fitted to calculations of P for various latitudes -

$$P = 1.32 + 4 \times 10^{-4} \Delta + 8 \times 10^{-5} \Delta^2 \quad (2)$$

This is not an empirical equation, based on measurements of radiation, but is simply shorthand for the theoretically determined value of P.

The fraction f of direct radiation in the ground's solar irradiance R_s depends on the cloudiness C. Hence the total direct component of solar irradiance, expressed in terms of the pan-water's area, is $f.P.R_s$, and the direct irradiance of the wall of the pan is $f.(P - 1).R_s$. As a first approximation, we may take f as proportional to the fraction of the sky that is not covered by cloud, eg $0.9(1 - C/8)$. Then an expression relating C to the attenuation of extra-terrestrial radiation R_a in penetrating to the ground (**Appendix 2**) allows f to be expressed as equal to $(2 R_s/R_a - 1.5)$.

b) Now consider the diffuse short-wave radiation on to the sides, which we will assume is isotropic. The amount depends on the fact that the wall is equally exposed to the sky above and the ground below, ie half of the wall's area is exposed wholly and exclusively to each source. As a result, the diffuse radiation from the sky consists of $0.5.(1 - f).R_s \times 0.97/1.15$, over the area of the water's surface. That equals $0.42(1 - f).R_s$.

c) The wall which half faces the ground receives reflected radiation from it, depending on the ground's albedo a. The latter may be as low as 11% for wet dark soil, or 18% when dry, or around 32% for a desert [19]. In humid regions the pan is usually surrounded by grass, with an albedo a of 0.22. In that case the reflected radiation received by the pan, expressed in terms of the water's area, is $0.09.R_s$ (ie $0.22 R_s \times 0.5 \times 0.97/1.15$) W.m⁻². In general, it is $0.42 a.R_s$ W.m⁻².K⁻¹.

The above three sections show that in total the augmented shortwave solar irradiance R_s of the pan is as follows -

$$\underline{R_s} = [1.42 + f(P - 1.42) + 0.42 a] R_s \quad \text{W.m}^{-2} \quad (3)$$

This shows that the ratio $\underline{R_s}/R_s$ equals 1.51 at all latitudes when f is zero (ie the sky is overcast) and a is 0.22, for example. On the other hand, if the sky is clear (ie f is about 0.9) and the latitude 60 $^{\circ}$, the ratio increases to 1.70. So values are about 1.6, in general.

d) Where the surroundings of a pan are dry, they are warmer, for lack of evaporative cooling. (The criterion of dryness is discussed below.) This leads to additional longwave radiation to the wall, amounting to $[(0.36.R_s - 36) / u]$ W.m⁻² (see **Appendix 3**).

There remains one more consideration, the effect of elevation on the ground's irradiation R_s . The intensity at sea level can be calculated in many ways [13], but most simply by two methods, A and B, described in a previous paper [12]. Then the result has to be multiplied by a height factor H, to allow for the thinner air layer above elevated sites. At sea level, the extra-terrestrial radiation R_a is reduced by a clear sky to about $0.75 R_a$ [13]. Therefore, at a height of 500 hPa (ie about 5,000 m) the reduction is to $0.87 R_a$, if it is regarded as approximately linearly related to height z. In other words, the radiation intensity R_s has to be increased by a factor H equal to $(1.0 + 3.2 \times 10^{-5} z)$, which differs significantly from unity if z is above about 600 m.

convective heat transfer to a pan

Whereas the convective heat-transfer coefficient h for water is $2.5 u$ W.m⁻².K⁻¹ [13], the coefficient for a small hard surface like the pan wall is about $4 u$ W.m⁻².K⁻¹ [20, 21]. So the pan areas mentioned earlier imply that the effective coefficient for the entire pan is $[1.15 \times 2.5 u + 0.97 \times 4 u] / 1.15$, ie about $6 u$ W.m⁻².K⁻¹, taken over the water's area. The enhanced heat exchange through the wall of a pan evaporimeter means that the effective sensible-heat transfer-coefficient ($6 u$ W.m⁻².K⁻¹) is greater than the latent-heat coefficient (ie $2.5 u$ W.m⁻².K⁻¹), confirming the findings of a preliminary study [22]. The resistance to the loss of heat by convection r_a is about $1200/6 u$ s.m⁻¹

(ie $r.c/h$, where r is the density of air and c its specific heat [12]), or $200/u$ s.m-1, varying slightly with temperature. On the other hand, the impedance to evaporation is about $480/u$ s.m-1 (ie $1200/2.5$ u). Thus, evaporation is effectively impeded by an extra resistance r_s of about $280/u$ s.m-1 (ie $480/u - 200/u$ s.m-1). These resistance values are used in **Appendix 4**.

In the present paper we use winds measured at 2 metres above the ground, since an US Class-A pan is often equipped with an anemometer at that height. Where winds are measured at other heights, they must be corrected. For instance, the wind at 2 m is about 0.73 times that at 10 m, or 1.6 times that at 0.5 m [13].

dry conditions

It was shown by Dale & Scheeringa [23] that dryness of the ground around a pan increases the evaporation rate. This may be attributed to the ground's longwave irradiance of the wall of a pan, considered already, and to the higher reflectivity of dry bare ground. There seems no other problem in applying Penman's equation in arid circumstances.

An area may be considered **dry** if the ground desiccates to the extent that vegetation dies. Such dryness occurs when the monthly precipitation P_r is much less than local lake evaporation - below half, say. The lake evaporation rate is roughly equal to $5 T$ mm per month, where T is the monthly mean Celsius temperature [13, 24], so it is proposed that a month is 'dry' if P_r below $2.5 T$. (This resembles Koeppen's criterion for a desert, ie P_r less than $[2.4 T + 12]$ mm/mo [25]). Alternatively, the area is arid if the annual rainfall is less than $30 T$, where T is the annual mean temperature.

The albedo of bare ground around a pan in arid country may be as high as 0.30, depending on the colour of the soil. If it is 0.30, the energy input to the pan is increased by $0.03 R_s W.m-2$ (ie $0.97 \times [0.30 - 0.22] R_s / 1.15$) on account of the albedo being higher than that of grass. But this is usually trivial.

the Penpan equation

Since the resistance impeding water loss from a pan is greater than that impeding heat transfer from the pan, the appropriate version of Penman's equation is the same as that for a leaf [26 - 30] -

$$L.E_p = \{R_n + r.c (T - T_d)/r_a\} / [1 + g (r_a + r_s)/s.r_a] \quad W.m^{-2} \quad (4)$$

where r_a (ie the resistance to heat loss) has already been shown to be $200/u$ s.m-1 and r_s (the additional resistance to water loss) is $280/u$ s.m-1. R_n is the net irradiance of the pan, r is the air's density, c its specific heat, g the psychrometric constant and s is the slope of the psychrometric curve near temperature T . The slope s can be calculated from an approximation [12]:-

$$s = [0.5 + 0.01 T + 0.0019 T^2] \quad hPa.K^{-1} \quad (5)$$

The net-irradiance term R_n in Eqn 4 is derived from a linear relationship with the solar irradiance R_s [13]. For a grass surface, R_n is given by $[0.63 R_s - 40] W.m-2$, and presumably $[0.8 R_s - 40]$ for a water surface because of its lower albedo [12]. The albedo of a pan is halfway between the respective values for water and green vegetation [13], so the appropriate expression is taken as $[0.71 R_s - 40] W.m-2$, where the value of R_s to take here is $H.R_s$, the augmented value adjusted for elevation.

Method

The outcome of the considerations above is the following version of Eqn 1, for the pan evaporation rate E_p at Melbourne, for instance (see Appendix 4) -

$$E_p = [21 T - 166 + 6 u (T - T_d)] / [28 + 46/s] \quad mm.d^{-1} \quad (6)$$

where T is the mean temperature, T_d the dewpoint, u the wind speed, and s the slope of the psychrometric curve at temperature T . This might be called the Penpan equation **for Melbourne**, and is as simple as Eqn 1.

Evaporation estimates have also been made for eight other widely-spaced places, within the range of 22 - 44 degrees of latitude (**Table 1**). The procedure for developing the Penpan equation for Merna (an elevated, occasionally dry place in Wyoming) is outlined in **Appendix 5**.

Results

Values from Eqn 5 are compared with measurements in **Fig 2**. The average error of monthly estimates is 0.49 mm.d-1, which is about 12% of the mean rate of 4.24 mm.d-1 measured by McIlroy & Angus [31] over three particular years.

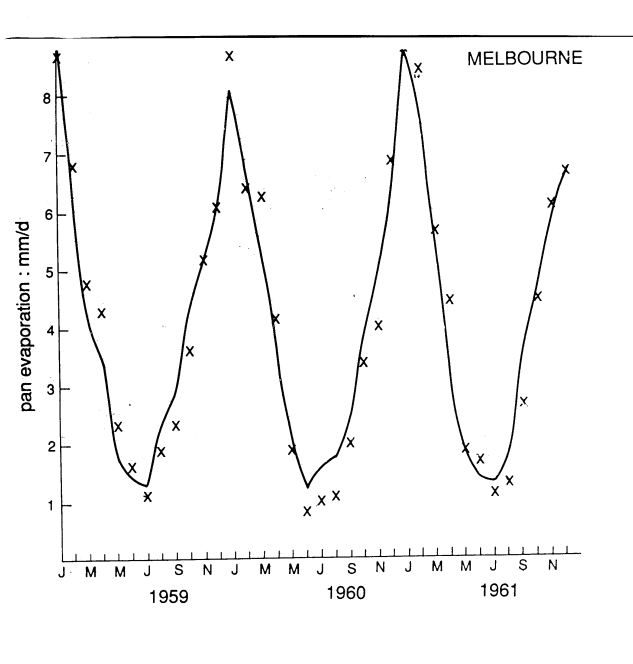


Fig 2. Comparison of estimates (crosses) from Eqn 5 with measurements (continuous line) obtained in 1959-1961 with a US Class-A pan evaporimeter at Melbourne [31]. .

The results from the eight other places are shown in **Fig 3**. The points lie much closer to a straight line than those in Fig 1. Also, deviations from the line representing equality of estimate and measurement are hardly proportional to the evaporation rate. This supports discussing estimate accuracy in terms of the average absolute, rather than the proportional error.

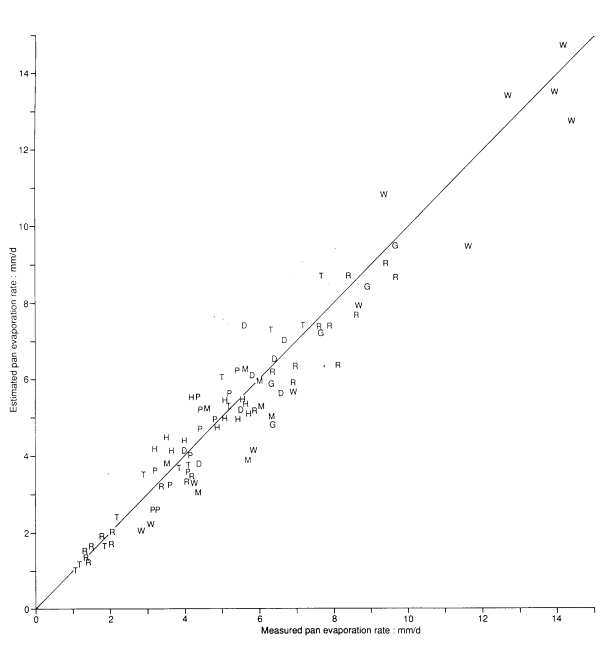


Fig 3. Comparison of estimated monthly mean evaporation rates with values measured at various places described in Table 1. The symbol D stands for Daniel (Wyoming), G for Gillette (Wyoming), H for Hong Kong, M for Merna (Wyoming), P for Pietermaritzburg (South Africa), R for Griffith (New South Wales), T for Mount Gambier (South Australia), W for Woomera (South Australia). The straight line shows where points lie if estimates equal measurements.

The median error in Table 1 is 0.55 mm.d-1, resembling the 0.49 mm.d-1 from Fig 2. In round terms, the error is about 0.6 mm.d-1, which is less than 10% of the midrange of Fig 3. Method B of estimating Rs yields lower evaporation-estimate errors in Table 1, except in the case of

Discussion

Obviously, the procedures described here are open to further refinement. The graphical method of deducing the dewpoint temperature [13] might be replaced by suitable equations, to facilitate spreadsheet calculation of evaporation rates. The pan factor P is preferably calculated for each month of the year, as the Sun's noon elevation changes. Also, allowance might be made for changes of daylength. The assumption of a linear attenuation of radiation, involved in the height factor H , is only an approximation. In addition, the estimation technique as a whole should be tested in an even wider range of latitudes and circumstances, and its use examined for periods shorter than a month.

As regards the accuracy of the estimates of evaporation, the absolute error is more useful than the percentage error. This is because evaporation values are subtracted from rainfall values, or from soil-moisture contents, in practice, and therefore errors are additive, not proportional [13].

The accuracy depends on the period of the estimate. At Melbourne the average rate of pan evaporation estimated over three years (using Method B and actual rainfall figures) is 4.12 mm.d-1, compared with a measured average of 4.24 mm.d-1 [31]. The difference of 3-year averages is only a quarter of the monthly error.

The above estimate of 4.12 mm.d-1 is the average of 36 monthly values. If, instead, the Melbourne Penpan equation is used with 3-year averages of the temperature, dewpoint and solar irradiance, the value obtained is 3.81 mm.d-1, which is further from the measured average. The superiority of an average of estimates over an estimate from averages has been discussed elsewhere [13].

It is notable that useful accuracy of estimation is achieved without the sort of empirical 'calibration' invoked by other authors [5, 32, 33] Also, errors of around 0.6 mm.d-1 are much better than can be claimed for the measurement of precipitation [13], with which evaporation has to be compared in assessing water gain or loss by soil or lake, for instance.

Most significantly, success in estimating pan evaporation from formulae based on Eqn 1 (which applies to lake evaporation), tends to validate that equation. That is more important in practice.

Conclusions

1. The ratio E_o/E_p is about 0.77, where E_o is the rate of evaporation from a lake and E_p from a US Class-A pan evaporimeter. However, this ratio varies with several factors, including the evaporation rate.
2. The value of E_p depends on the solar irradiance R_s of the pan, which in turn depends on the pan's geometry, latitude, elevation and solar declination, and the amount of cloud. These factors have been allowed for in developing equations based on Penman's formula, for estimating E_p .
3. Dryness of bare ground around a pan alters the albedo and temperature of the surface, and hence also affects the pan's irradiance, ie its evaporation rate. Such dryness is indicated by a monthly rainfall (mm) less than 2.5 times the mean temperature (oC).
4. A so-called Penpan equation for estimating pan evaporation, based on method A of estimating solar radiation, requires only temperature data as essential input, though wind data are desirable in addition. However, it is less accurate than an equation based on method B, involving extra-terrestrial radiation and rainfall measurements. In general, the error of estimation is around 0.6 mm.d-1.

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Appendix 1 Papers showing the ratio of lake evaporation to that from a US Class A pan evaporimeter

Young [34] (77%, 77%), Penman [10] (78%), Kohler et al. [6] (60% - 82%), Harbeck [35] (69%), Nordensen & Baker [36] (74%), Nimmo [37] (61% - 79%), Sellers [38] (82%), Webb [39] (70%), Stanhill [40] (67%), Stanhill [16] (70%), Allen & Crow [7] (75% - 78%), Ficke [41] (76%), Hounam [8] (72%, 80%), Neuwirth [42] (72%), Hoy [43] (78%), Garrett & Hoy [44] (63% - 94%), Linsley et al. [45] (73%, 71%), Duru [46] (79%).

Appendix 2 The effect of cloudiness on the fraction f of solar radiation which is direct

It has been shown elsewhere [13] that the extra-terrestrial radiation R_a is reduced to the ground-level value R_s according to the cloudiness, approximately as follows -

$$R_s = R_a (0.85 - 0.047 C) \text{ W/m}^2 \quad (2.1)$$

$$\text{Hence } C = (0.85 - R_s / R_a) / 0.047 = 18 - 21 R_s / R_a$$

$$\text{Thus the fraction } f = 0.9 (1 - C/8) = 2 R_s / R_a - 1.5$$

Appendix 3 The additional longwave irradiance of the pan wall in dry surroundings

There is a net transfer of longwave radiant heat between the ground and the side of a pan, because of any temperature difference. A difference arises from a lack of any evaporative cooling of the ground, when the climate is arid. In that case, all the net irradiance of the ground's surface R_g is converted into upwards convection of sensible heat (apart from daily cyclic flows between the surface and lower levels of the ground). Consequently, there is a warming of the surface by R_g/h' , where h' ($\text{W.m}^{-2}\text{.K}^{-1}$) is the heat transfer coefficient between the air and the ground. The coefficient depends on the ground's roughness, but is typically about $4 u \text{ W.m}^{-2}\text{.K}^{-1}$ [13].

The value of R_g is $[(1 - a) R_s - (107 - T - 9 C)] \text{ W.m}^{-2}$, where a is the ground's albedo, T the mean temperature of the air, and C the cloudiness in oktas [13]. Typical values in arid conditions for a , T and C are 0.3, 20°C and 2, respectively. In this case, R_g equals about $[0.7 R_s - 69] \text{ W.m}^{-2}$, and the warming of the ground R_g/h' is $[0.17 R_s - 17]/u$ degrees.

Pan-wall and air temperatures are similar, because of the evaporation from the water surface. The net longwave flux between surfaces which face each other is about 5 W.m^{-2} for each degree difference [13, 47], but this has to be halved in the case of a pan, because in effect only half the wall faces the ground, being at right-angles to it. So, for each degree difference, there is a flux (in terms of the pan's water-surface area) of about 2.1 W.m^{-2} (ie $0.5 \times 5 \times 0.97/1.15$). Thus, the extra longwave irradiance from a bare dry environment L_i is $[(0.36 R_s - 36) / u] \text{ W.m}^{-2}$. Such is the extra longwave irradiance to be considered when conditions are dry, to be added to the calculated net irradiance of the pan.

Appendix 4 Deriving a Penpan equation

In view of the various considerations above, Eqn 4 becomes the following -

$$E_p = [R_n + 6 F u (T - T_d)] / [28 + 68 g / s] \text{ mm.d}^{-1} \quad (4.1)$$

where F is the same as in Eqn 1. The number 68 is $28.4 \times (200 + 280)/200$, and 28.4 arises from the conversion of units from W.m^{-2} to mm.d^{-1} . The net irradiance R_n is $[0.71 R_s + L_i - 40] \text{ W.m}^{-2}$, as discussed in the text, where L_i is the longwave increment (Appendix 3).

The procedure for deriving g and F in the above expression, and for obtaining P and f in calculating R_s , is demonstrated below, for the case where the only data available are the latitude (A), altitude (z metres), distance inland (d kilometres), the (approximate) wind speed (u metres per second) and the daily extreme temperatures. If there are additional data on dewpoint, monthly rainfall, cloudiness or solar irradiance R_s , these can be used in place of approximations based on monthly-mean daily-extreme temperatures alone.

As an example, values (shown bold) are derived at each stage for the case of a pan at Melbourne. This is at latitude 38°S , near sea level and about 60 km downwind of the ocean. The annual mean temperature there T is 16.0°C .

i) Derive g from the following [12]:- $g = [0.67 - 7.2 \cdot 10^{-5} z] \text{ hPa.K}^{-1}$ **0.67**

ii) Calculate F from the following [12]:- $[1.0 - 8.7 \cdot 10^{-5} z]$ **1.0**

iii) Reckon f as 0.2, 0.5 or 0.8 according to whether the month's weather is wet and cloudy, average or dry, respectively. **0.5**

iv) Obtain P from Eqn 2:- $[1.32 + 4 \times 10^{-4} A + 8 \times 10^{-5} A^2]$ **1.44**

v) Allot an albedo value a to the ground around the pan, according to the degree of grass cover and its dryness [13], eg 0.22 for well-watered grass and about 0.30 for dry bare ground. **0.22**

vi) Hence derive R_s/R_a from Eqn 3 **1.52**

vii) Use the above ratio to determine R_s from an estimate of the monthly mean solar irradiance of the ground R_a obtained by one of the methods described elsewhere [12, 13], as follows -

Method A

If only daily extreme temperatures are available, take their average as the daily mean, whose average over a month is T . Hence find the annual mean T . **16.0**

Then deduce the approximate annual mean irradiance R_y from the following [12, 48]:-

$$[210 + 1.8 \underline{A} - 0.06 \underline{A}^2] \text{ W.m-2 } \mathbf{191^*}$$

(*This agrees with the measured three-year average of 193 W.m-2 reported by McIlroy & Angus [31]).

Next derive the annual range of monthly mean temperatures DT, either from measurements (which is preferable) or from this approximate relationship with latitude and distance downwind of the ocean (d km) [12]:-

$$DT = 0.13 \underline{A} d^{0.2} \text{ degrees } \mathbf{11}$$

Also calculate the annual range of irradiance DR, using the following empirical approximation [12] :-

$$DR = [60 + 4 \underline{A}] \text{ W.m-2 } \mathbf{212}$$

Hence the month's deviation of irradiance q from the annual mean is as follows [12]:-

$$q = DR (T - \mathbf{T}) / DT \text{ W.m-2 } \mathbf{[19.3 T - 308]}$$

The monthly mean solar irradiance Rs at sea level is Ry plus q

$$\text{W.m-2 } \mathbf{[19.3 T - 117]}$$

This needs adjustment for elevation (z metres), i.e. multiplication by the height factor H, equal to $(1.0 + 3.2 \times 10^{-5}z)$ **1.0**

Method B

This is more accurate than Method A, because it incorporates additional information on monthly rainfall Pr mm, replacing temperature as the proxy for irradiance measurements. Method B also involves the cloudiness C (in tenths, approximately equal to $[1 + 0.5 \log Pr + \{\log Pr\}^2]$) and the extra-terrestrial radiation Ra, published in a table for any particular month and latitude [13]. The solar irradiance Rs is approximately as follows [13]:-

$$Rs = [Ra (0.85 - 0.047 C)] \text{ W.m-2 } \mathbf{(4.2)}$$

viii) Now correct for the reduced attenuation of the atmosphere above sites higher than 600m, by multiplying by the height factor H, given above.

ix) The radiation to a pan involves an augmentation of Rs by a factor given by Eqn 3, as mentioned in the text. So the corrected, augmented irradiance Rs is this for Melbourne:-

$$\underline{Rs} = [Ra (0.85 - 0.047 C)] [1.0 + 3.2 \times 10^{-5}z] [1.42 + f(P - 1.42) + 0.42 a] \text{ W.m-2 } \mathbf{[29.3 T - 178]}$$

x) Hence derive Rn for Eqn 4, i.e. $[0.71 \underline{Rs} - 40]$ W.m-2 **[21T - 166]**

But add $[0.36 Rs - 36]/u$ to the above value of Rn to allow for longwave radiation onto the walls of the pan, if the area is arid. This is the case when either the monthly rainfall is less than 2.5 T mm (where T is the monthly mean temperature), or the annual rainfall is below 30 T mm (where T is the annual mean).

xi) The expression above can be put into Eqn 4.1 to yield Eqn 6 in the text:-

$$Ep = [21 T - 166 + 6 F u (T - Td) / \{28 + 46/s\}] \text{ mm.d-1}$$

Appendix 5 Derivation of the Penpan equation for Merna in Wyoming

This involves the use of Method A for determining the solar irradiance, at a high elevation, with aridity in some months.

The latitude of Merna is 43oN, so Ry is 176 W.m-2, P 1.48 and DR 232 W.m-2. The elevation is 2,377 m, so g is 0.50 (therefore 68g equals 34), F is 0.793 (so 6 F is 4.8) and H is 1.08. The annual range DT is 25.4K. Monthly rainfalls exceed 2.5 T, so f is 0.5 and the pan is surrounded with grass, and therefore the environs' albedo is 0.22. Hence -

$$Ep = [0.71 \underline{Rs} - 40 + 4.8 u F (T - Td) / \{28 + 34/s\}] \text{ mm.d-1 } \mathbf{(5.1)}$$

$$\text{where } \underline{Rs} = 1.08 Rs (1.42 + P f - 1.42 f + 0.42 a) = 1.54 Rs \text{ W.m-2 } \mathbf{(5.2)}$$

$$\text{where } Rs = Ry + DR(T - \mathbf{T})/DT \text{ W.m-2 } \mathbf{(5.3)}$$

The monthly temperatures indicate that T is 1.3 oC. Hence:-

$$Rs = 176 + 232 T/25.4 - 232 \times 1.3/25.4 = 9.9 T + 177 \text{ W.m-2 } \mathbf{(5.4)}$$

$$\text{Thus, the augmented irradiance } \underline{Rs} = 1.54 Rs = 15.2 T + 272 \text{ W.m-2 } \mathbf{(5.5)}$$

$$\text{Hence, the net irradiance:- } Rn = 0.71 \{15.2 T + 272\} - 40 = 10.8 T + 153 \text{ W.m-2 } \mathbf{(5.6)}$$

This must be increased by the additional longwave irradiance in the two months reckoned as dry, ie by $[0.36 (9.9 T + 177) - 36]/u$,

$$\text{i.e. by } [3.6 T + 28]/u = Li \text{ W.m-2 } \mathbf{(5.7)}$$

$$Ep = [10.8 T + 153 + Li + 4.8 u (T - Td) / \{28 + 34/s\}] \text{ mm.d-1 } \mathbf{(5.8)}$$

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Table 1. Details of the places mentioned in Fig 3. The elevation is given in metres, the rainfall in millimetres per annum and the mean estimation error for each place in mm.d-1.

place	latitude	elevation	height of wind meter	screen over pan?	years of data	annual rain:mm	Rs Method	mean error	source
Daniel	43	2195	2	no	1984 -85	-	A	0.56	L.O.Pochop,Univ. of Wyoming
Gillette	44	1389	2 (1)	no	1931-75	388	A	0.60	[3]
Griffith	34	125	10	no	1960-1	411	B	0.45	[50]
Hong Kong	22	33	0.5	no	1958-75	2303	B	0.53	[51]
Merna	44	2377	2	no	1984-85	-	A	0.89	L.O.Pochop,Univ. of Wyoming
Mount Gambier	38	63	10	yes	1980	712	B	0.36	Aust. Bureauof Meteorol.
Pietermaritzburg	30	1076	2	yes	1980	567	B	0.54	B.Clemence,Dept. Agric.,S. Africa
Woomera (2)	31	165	10	yes	1980	79	B	1.08	Aust. Bureauof Meteorol.

(1) assumed

(2) the pan was surrounded by a light-coloured gravel

SYMBOLS

Δ - the latitude (degrees)

a - the albedo, ie shortwave-radiation reflectivity

C - the cloudiness C expressed in \diamond oktas \diamond , ie in units of eighths of the sky \diamond s area

C - the fraction of the sky occupied by cloud (oktas)

c - the specific heat of air, ie the amount of heat required to warm unit mass by one degree Celsius

d - day, eg $\text{mm}\cdot\text{d}^{-1}$ means millimetres per day

d - the distance (in kilometres) upwind to an ocean shore

DR - the difference between the monthly mean values of solar radiation R_s in the months with least and most, respectively

DT - the difference between the monthly mean temperatures of the hottest and coldest months, respectively

Eo - the evaporation rate of a lake ($\text{mm}\cdot\text{d}^{-1}$)

Ep - the evaporation rate of a US Class-A pan evaporimeter ($\text{mm}\cdot\text{d}^{-1}$)

EPen - the lake evaporation rate estimated from Penman's formula ($\text{mm}\cdot\text{d}^{-1}$)

Et - the evaporation rate of a well-watered crop, ie the potential crop evaporation rate ($\text{mm}\cdot\text{d}^{-1}$)

F - a factor equal to $[1.0 - 8.7 \times 10^{-5} z]$, expressing the effect of elevation on atmospheric density, and hence on the convection of heat from a surface

f - the proportion of the solar radiation R_s which is direct from the Sun

g - the psychrometric constant, about $0.67 \text{ hPa}\cdot\text{K}^{-1}$ at sea level, but less at higher elevations

H - the factor $[1.0 + 3.2 \times 10^{-5} z]$, expressing the effect of elevation on the solar radiation R_s

h - the convective heat-transfer coefficient, being a measure of the rate at which heat energy is transferred through unit area by convection

h_c - the coefficient of heat transfer between the ground and the atmosphere

hPa - hectopascal, the unit of atmospheric pressure (replacing the millibar)

K - degree Celsius difference

K^{-1} - per degree Celsius

L - the latent heat of water evaporation, ie the amount required to evaporate unit mass (Joules per kilogram)

L_i - the extra longwave irradiance from a bare dry environment

m - metres

mm - millimetre

mo^{-1} - per month

P - the pan radiation factor, expressing the effect of the pan's geometry on the solar radiation it intercepts, as a daily average

P_r - the monthly precipitation (mm)

Q - the angle of the Sun above the horizon, ie the Sun's elevation

q - the difference between a month's mean sea-level solar irradiance and the annual mean

r - the density of air

R_a - the extra-terrestrial radiation intensity, ie the intensity of solar radiation above the atmosphere, onto a surface parallel to the ground

r_a - the resistance to either heat loss from a flat surface to the atmosphere

R_g - the value of R_n for ground's surface

R_n - the net irradiance of a surface, being the difference between the incoming (shortwave and longwave) radiation and outgoing (reflected and emitted) radiation

R_s - daily mean solar irradiance of the ground

R_{sl} - the value of R_s at sea level

$\underline{R_s}$ - the augmented shortwave solar radiation, ie the sum of the three component fluxes to a US Class-A pan, viz the direct, the diffuse and the reflected fluxes

r_s - the extra resistance (in addition to r_a) impeding evaporation from a US Class-A pan, since evaporation takes place only from the water surface, whereas heat is lost more easily, from the walls of the pan also

R_y - the annual mean solar irradiance

s - the slope of a tangent to the psychrometric curve, a graph of saturated water-vapour pressure against temperature

$\text{s}\cdot\text{m}^{-1}$ - seconds per metre, a unit of the resistance to heat transfer

T - daily mean Celsius temperature

T - the annual mean temperature

Td - the daily mean dewpoint temperature

u - daily mean wind speed (metres per second)

W.m⁻² - watts per square metre, a unit of energy flux

z - elevation (metres)

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